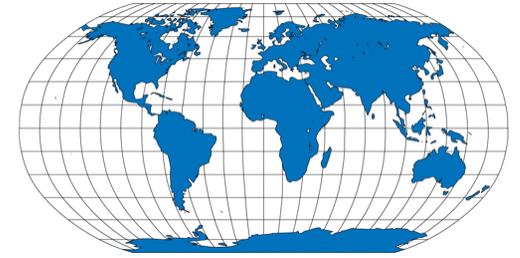


MAP PROJECTIONS



Map Projections



Session Objectives:

At the conclusion of this session, you will be able to:

- Develop a rudimentary knowledge of map projections and datums.
- Minimize distortion in map projections.
- Understand the difference between map projections and coordinate systems.
- Choose the appropriate projection and datum for your map.

Datums, Projections, and Coordinate Systems

- “be afraid, be very afraid”

Coordinate Conversion: Cartesian (ECEF X, Y, Z) and Geodetic (Latitude, Longitude, and Height)

Direct Solution for Latitude, Longitude, and Height from X, Y, Z

This conversion is not exact and provides centimeter accuracy for heights < 1,000 km
(See Bowring, B. 1976. Transformation from spatial to geographical coordinates. Survey Review, XXIII: pg. 323-327)

$$\phi = \text{atan}\left(\frac{Z + e'^2 b \sin^3 \theta}{p - e'^2 a \cos^3 \theta}\right)$$

$$\lambda = \text{atan2}(Y, X)$$

$$h = \frac{p}{\cos(\phi)} - N(\phi)$$

where:

ϕ, λ, h = geodetic latitude, longitude, and height above ellipsoid

X, Y, Z = Earth Centered Earth Fixed Cartesian coordinates

and:

$$p = \sqrt{X^2 + Y^2} \quad \theta = \text{atan}\left(\frac{Za}{pb}\right) \quad e'^2 = \frac{a^2 - b^2}{b^2}$$

$$N(\phi) = a / \sqrt{1 - e'^2 \sin^2 \phi} = \text{radius of curvature in prime vertical}$$

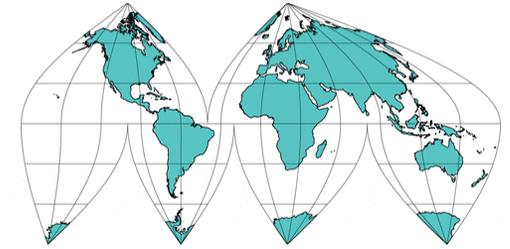
a = semi - major earth axis (ellipsoid equatorial radius)

b = semi - minor earth axis (ellipsoid polar radius)

$$f = \frac{a - b}{a} = \text{flattening}$$

$$e'^2 = 2f - f^2 = \text{eccentricity squared}$$

Map Projections



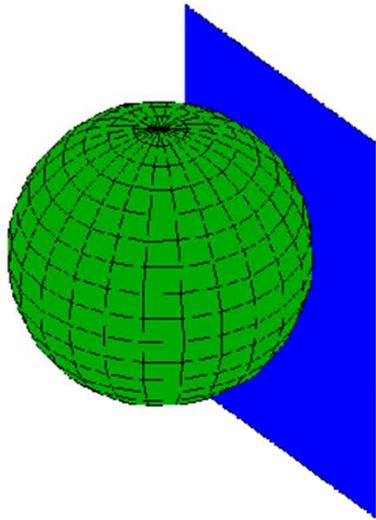
A spherical surface cannot be flattened without distorting it in several ways, so all maps must select and arrange distortions by means of a systematic transformation called a ...

map projection

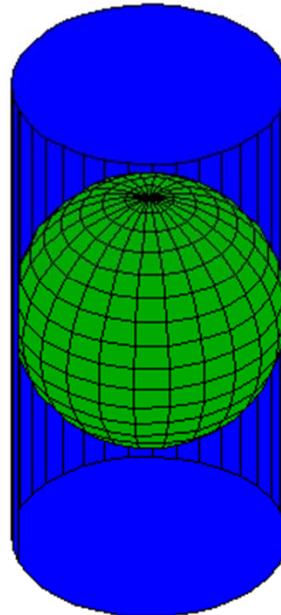
Map Projections

Projection Surfaces

Peter H. Dana 9/20/94



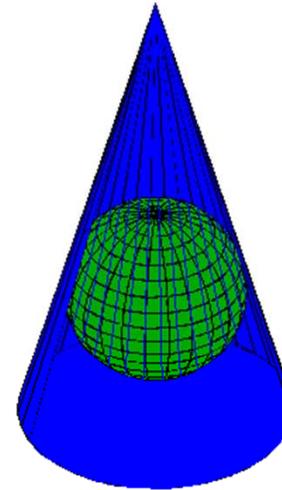
Planar Projection Surface



Cylindrical Projection Surface

Peter H.

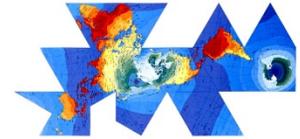
Peter H. Dana 9/20/94



Conical Projection Surface

Map Projections

Distortion

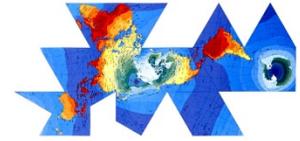


Projecting data from a 3-dimensional surface to a 2-dimensional surface introduces ...

distortion

Map Projections

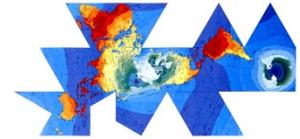
Kinds of Distortion



- **Shape**
- **Area**
- **Distance**
- **Direction**

Map Projections

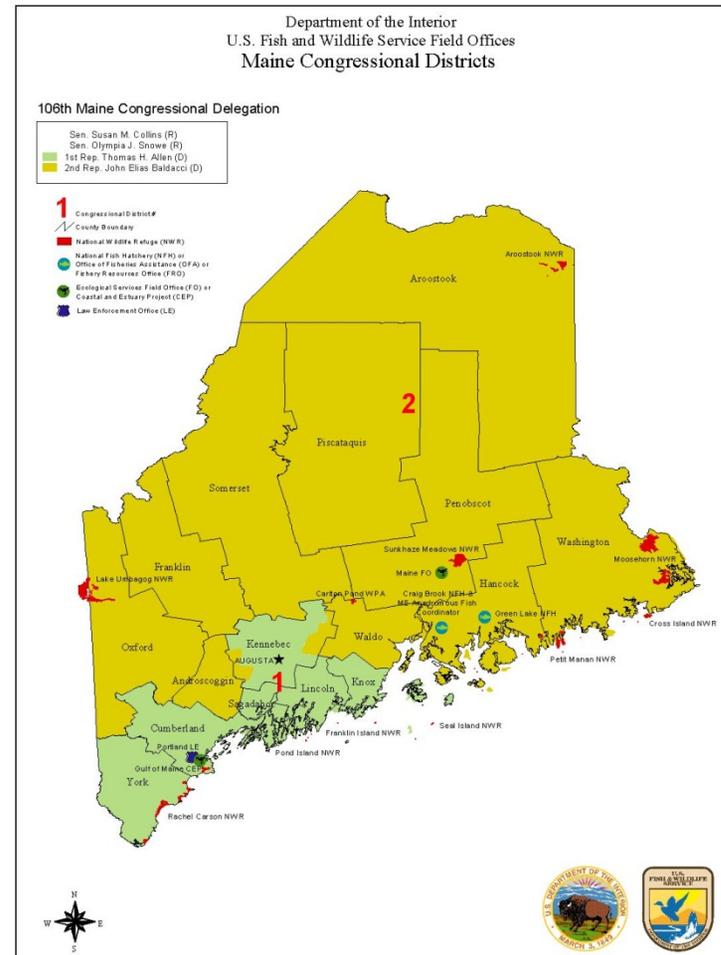
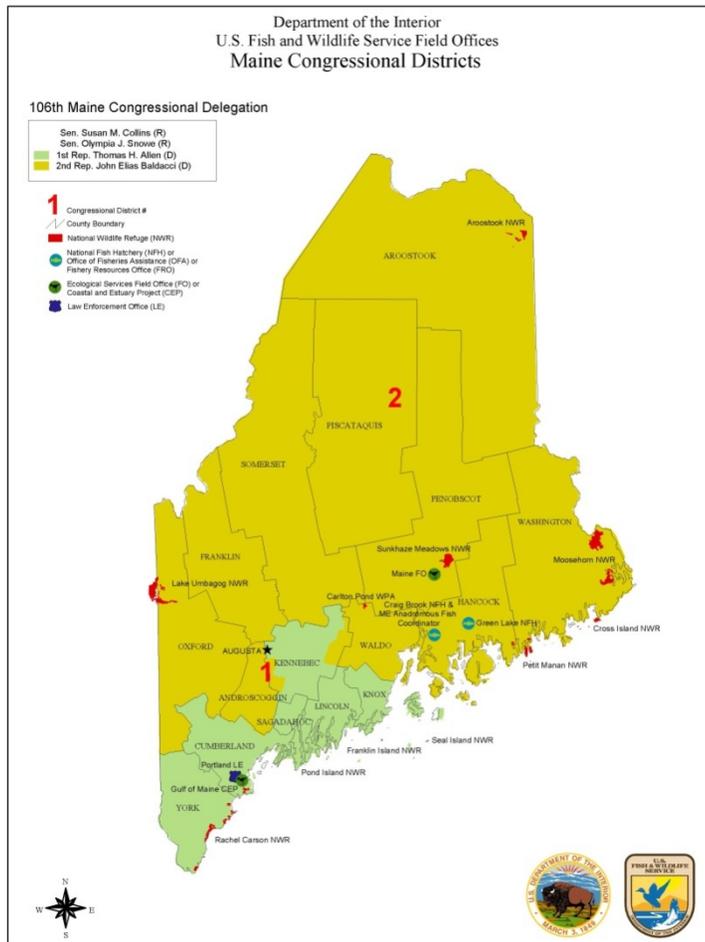
Correcting Distortion



- **Shape** : conformal projection
- **Area** : equal-area projection
- **Distance** : equidistant projection
- **Direction** : azimuthal projection

Map Projections

Distortion Example



Map Projections

Three Map Projections Centered at 39 N and 96 W

Mercator

Lambert Conformal Conic



Un-Projected Latitude and Longitude

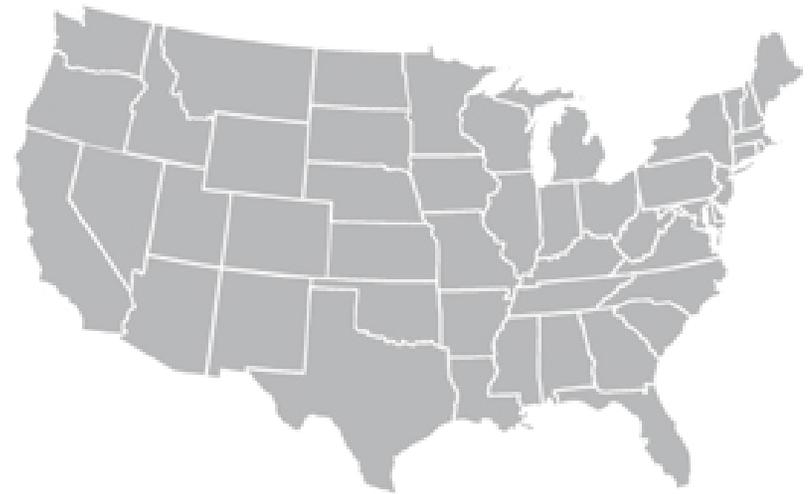
Peter H. Dana 6/23/97

Map Projections

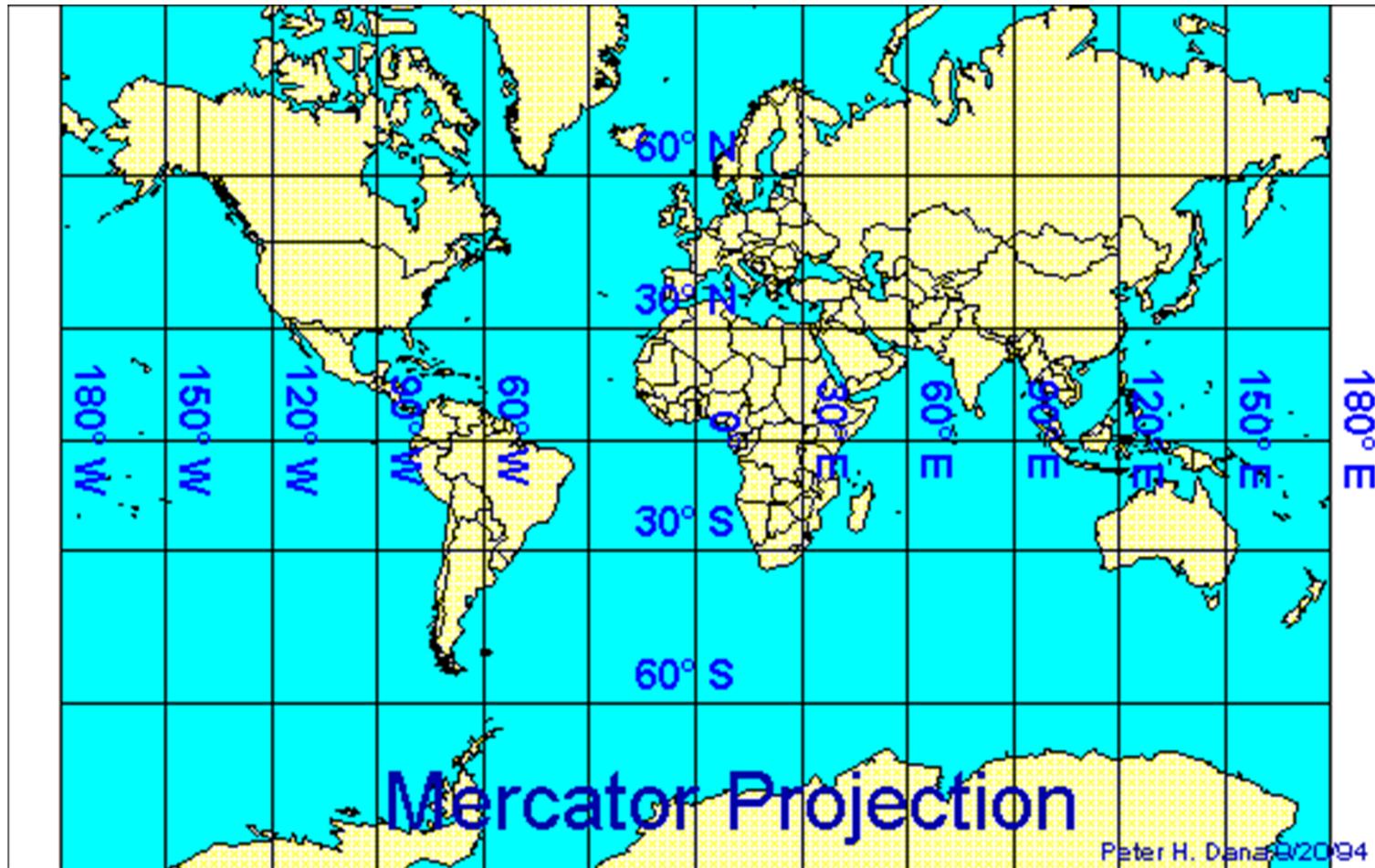
LAMBERT



ALBERS



Map Projections



Map Projections

Area Distortion

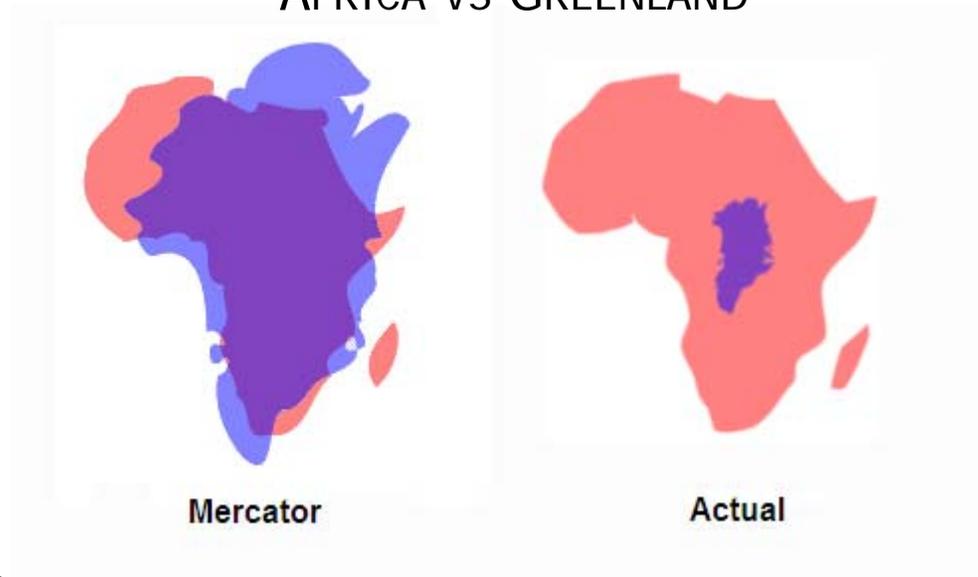
MERCATOR PROJECTION

Europe : 4 million square miles



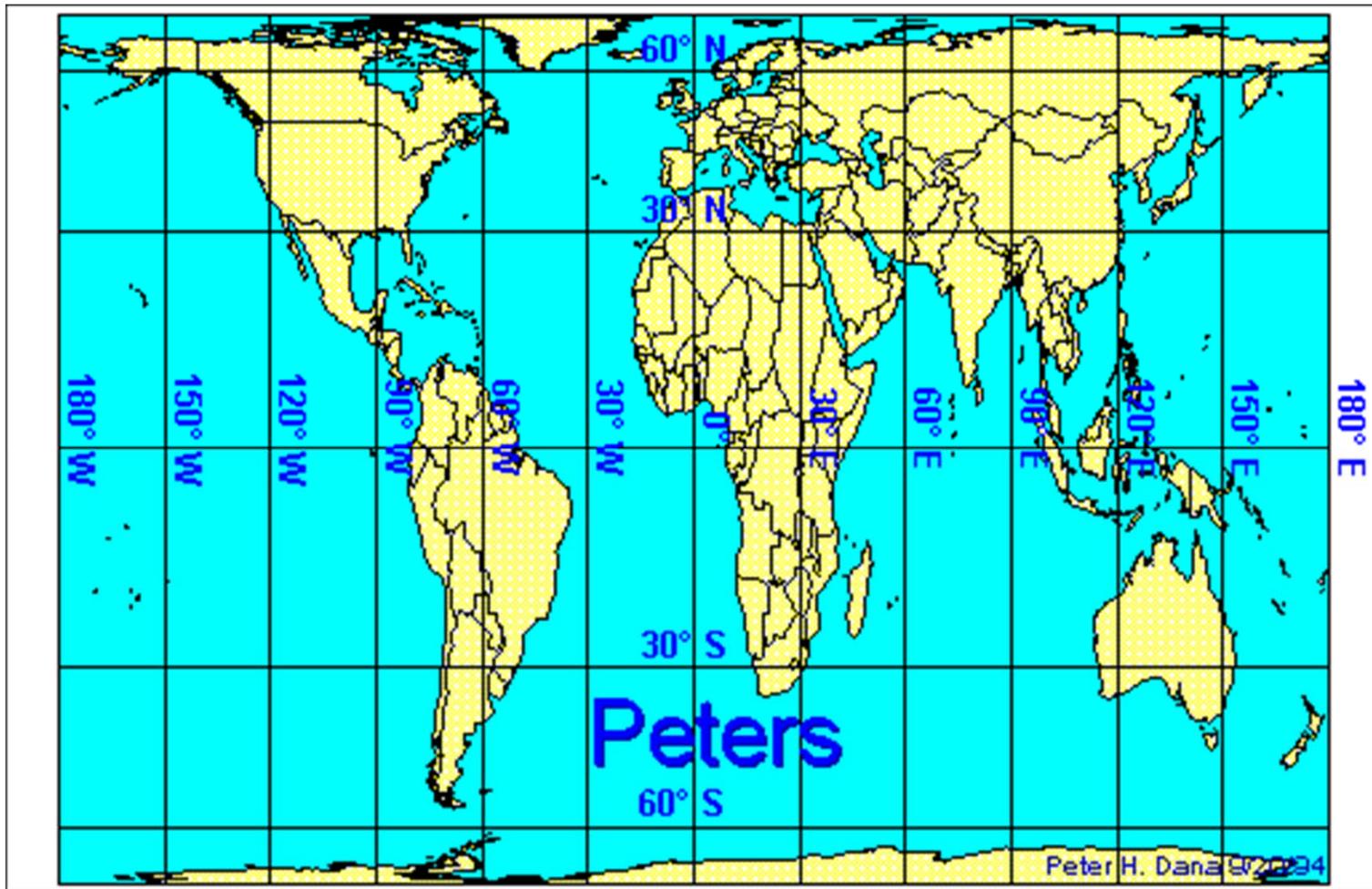
South America : 7 million square miles

AFRICA VS GREENLAND



Map Projections

Correcting Distortion



Map Projections

UTM – Universal Transverse Mercator

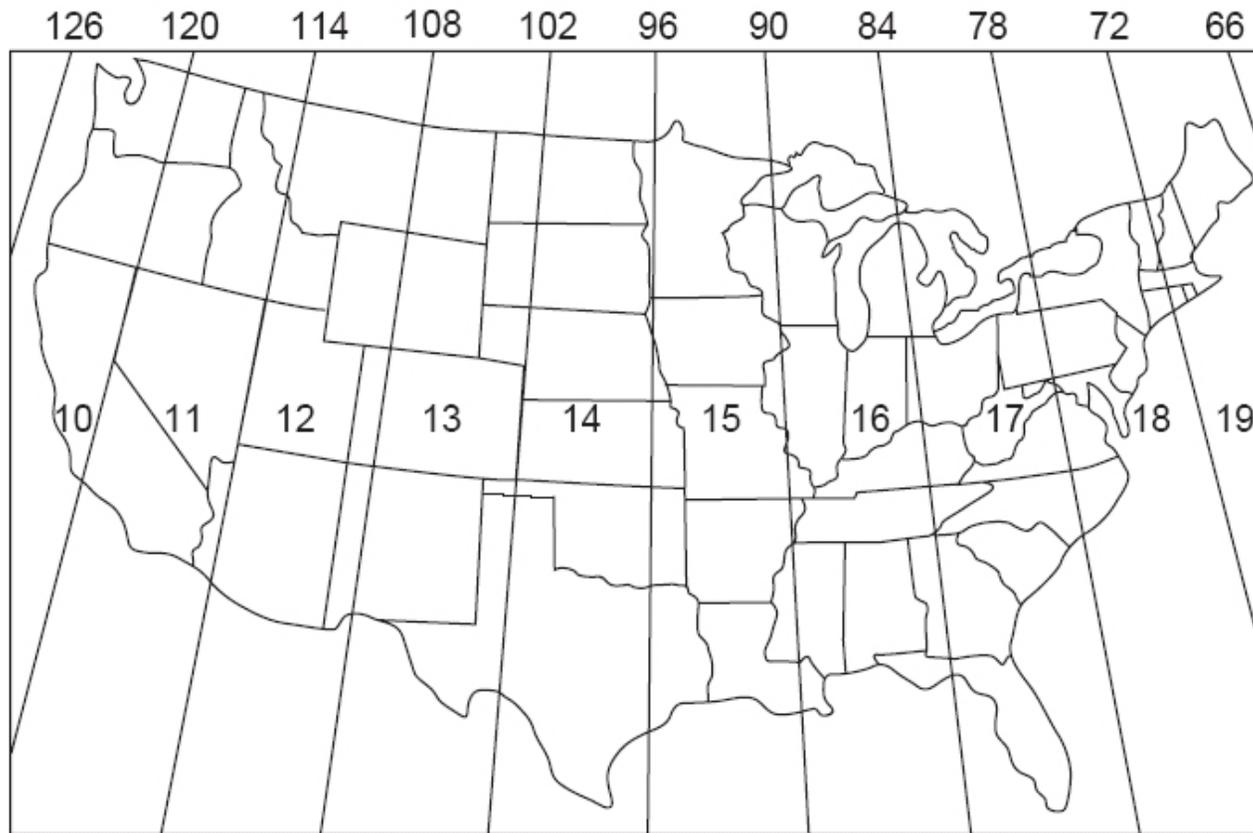
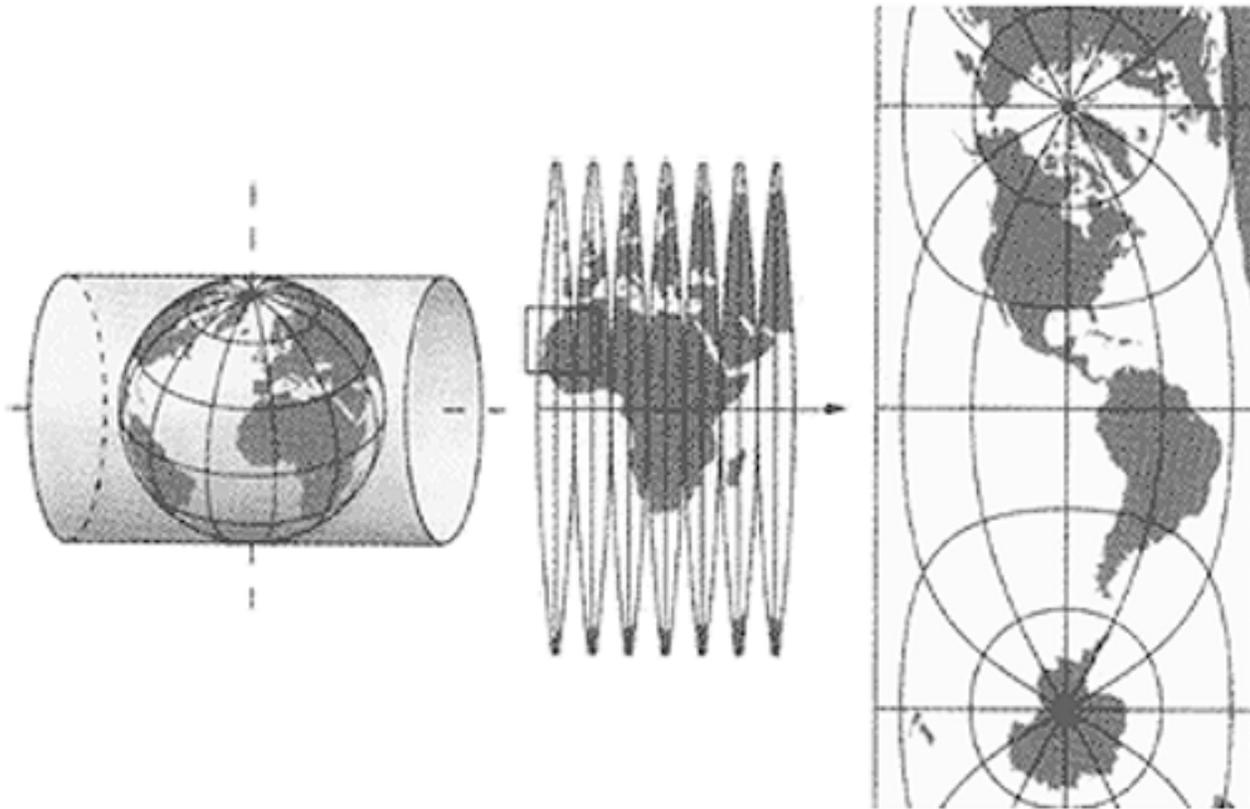


Figure 1. The Universal Transverse Mercator grid that covers the conterminous 48 United States comprises 10 zones—from Zone 10 on the west coast through Zone 19 in New England.

Map Projections

UTM – Universal Transverse Mercator



Map Projections

State Plane Coordinate System



Map Projections

State Plane Coordinate System

Projected Coordinate System:

NAD_1983_StatePlane_Tennessee_FIPS_4100_Feet

Projection: Lambert_Conformal_Conic

False_Easting: 1968500.00000000

False_Northing: 0.00000000

Central_Meridian: -86.00000000

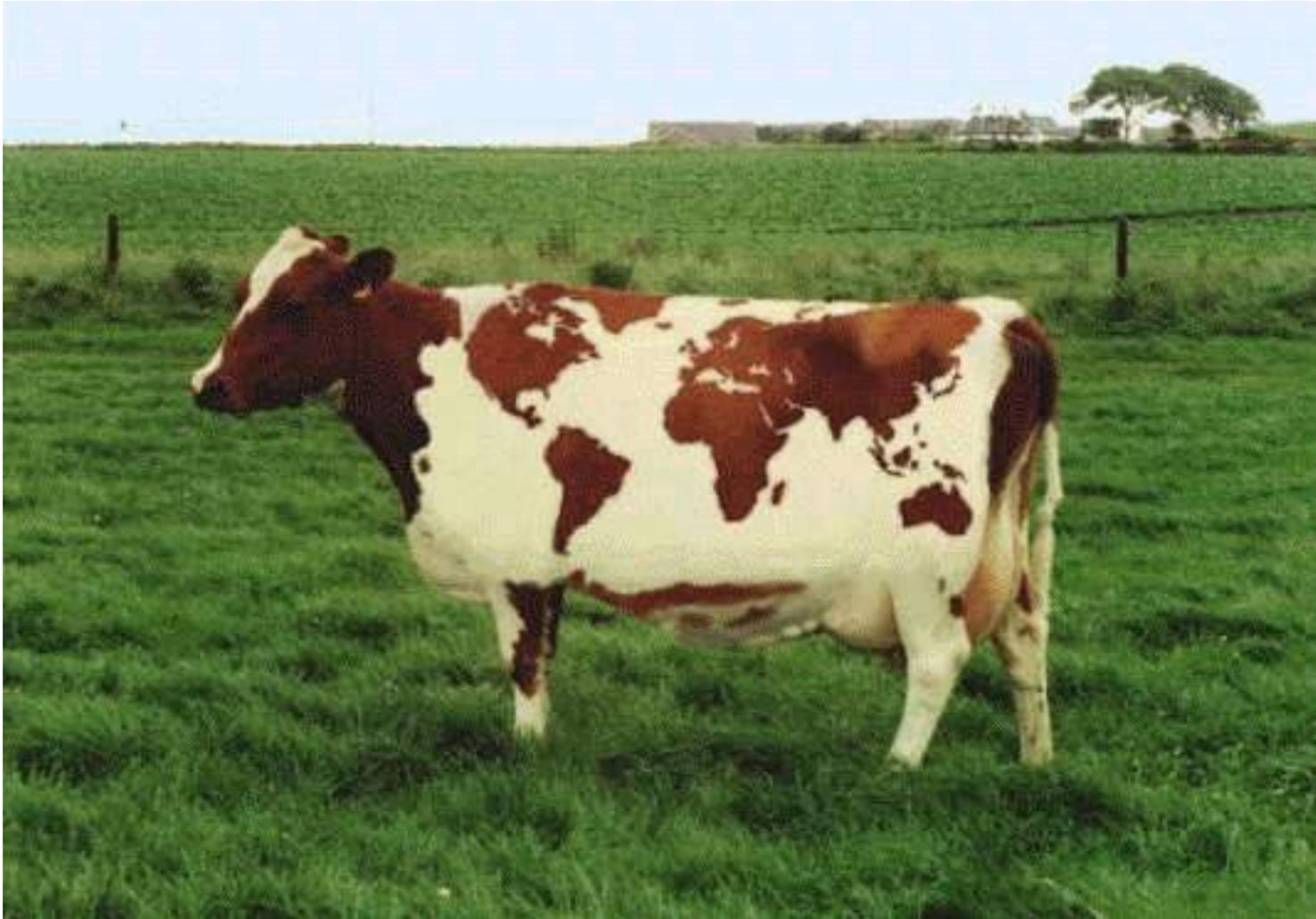
Standard_Parallel_1: 35.25000000

Standard_Parallel_2: 36.41666667

Latitude_Of_Origin: 34.33333333

Linear Unit: Foot_US

Map Projections



Map Projections

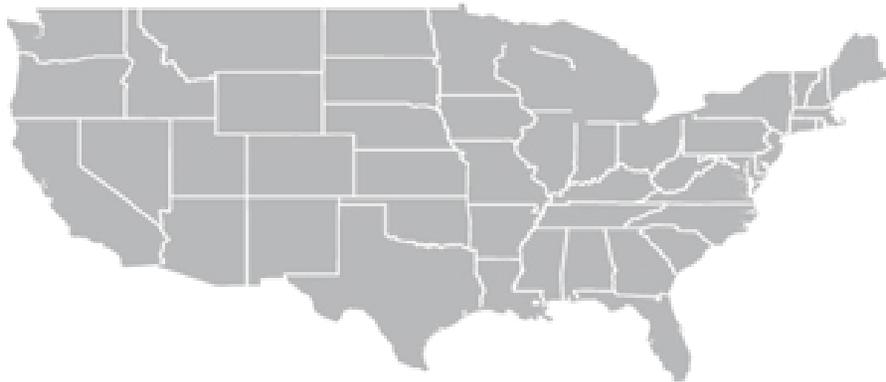
How this fits into Map Design

- You should choose a map projection that relegates distortion to places on your map that are not important to your message.
- At small scale, your projection choice will determine the overall “look” of your map.

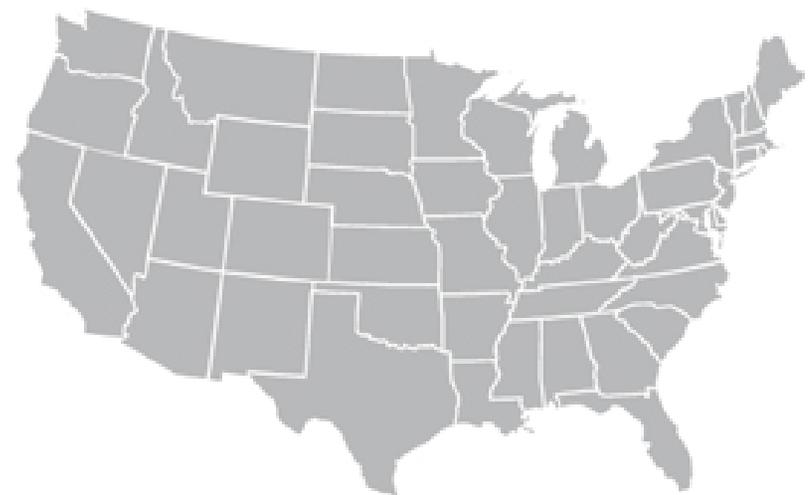
Map Projections

How this fits into Map Design

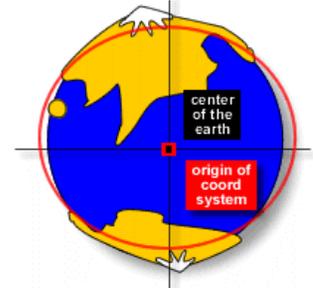
GEOGRAPHIC



ALBERS

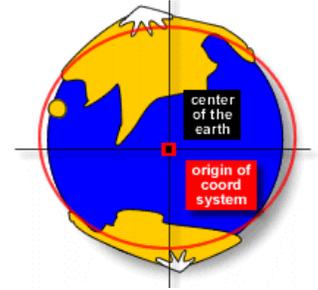


Datums



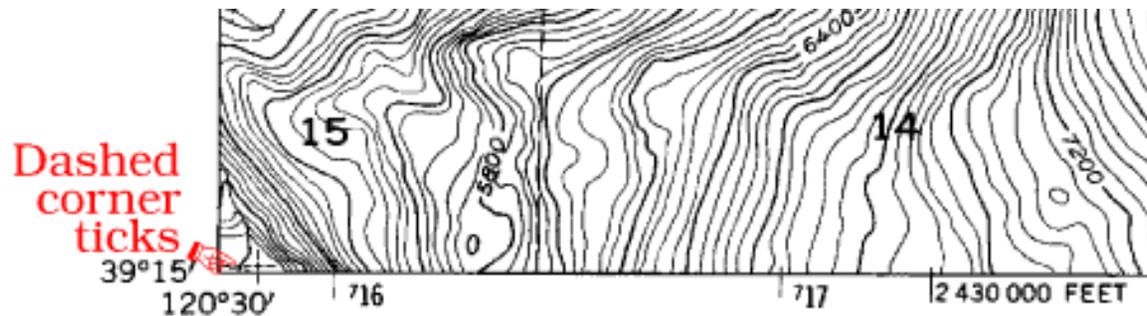
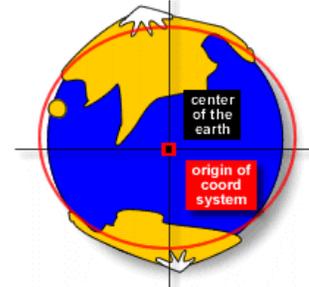
- **Wikipedia:** A datum is a reference point on the earth's surface against which position measurements are made, and an associated model of the shape of the earth for computing positions.
- **National Geospatial Intelligence Agency:** A datum is a point, a line, or surface used as a reference in surveying and mapping. A geodetic datum is a mathematical model of the earth used to calculate the coordinates on any map.

Datums



- NAD-27 : Clarke's 1866 ellipsoid
(best-fitted for the United States)
- NAD-83 : 1980 Geodetic Reference System
GRS 80 (best fitted for the entire Earth)

Datums



Mapped, edited, and published by the Geological Survey

Control by USGS and NOS/NOAA

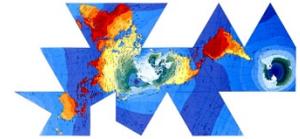
Topography from aerial photographs by multiplex methods
Aerial photographs taken 1953. Field check 1955

 **Map datum**

Polyconic projection. [1927 North American datum](#)
10,000-foot grid based on California coordinate system, zone 2
1000-meter Universal Transverse Mercator grid ticks,
zone 10, shown in blue

Datum offset 

To place on the predicted North American Datum 1983
move the projection lines 15 meters north and
89 meters east as shown by the dashed corner ticks



Some final advice...

- Making a small scale map to display geographic features? Use a conformal projection such as Lambert Conformal Conic
- Making a map to perform area calculations? Use an equal area projection like Albers Equal Area.